

# Tutorial: Integrating Object-oriented Design and Deductive Verification of Software

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[www.key-project.org](http://www.key-project.org)

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## Part I

### Intro, Overview, Architecture


## What is this Tutorial all About?

It is about an *approach* and *tool* for the

- ▶ **Design**
- ▶ **Formal specification**
- ▶ **Deductive verification**

of

- ▶ **OO software**

The *approach*, *tool*, and *project* is named 

in the following: 'KeY'

## KeY Project Partners



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## Some Buzzwords Early On

- ▶ **Java** as target language
- ▶ **Dynamic logic** as program logic
- ▶ Verification = **symbolic execution** + **induction**
- ▶ **Sequent style** calculus + meta variables + incremental closure
- ▶ **Interactive prover** with advanced UI
- ▶ Deep integration with two standard SWE tools:
  - ▶ **TogetherCC**, a commercial CASE tool
  - ▶ **Eclipse**, an open extensible IDE
- ▶ Specification languages
  - ▶ **JML**
  - ▶ **OCL/UML**
- ▶ **Smart cards** as main target application

## First Demo

## A first 'Kick & Rush' Demo

Intention:

- ▶ **First impression, look & feel**
- ▶ **Motivate tutorial issues**
- ▶ But for now:
  - ▶ *No details*
  - ▶ *Few explanations*

More [Demos](#) to come

## What Have You (and What Have You NOT) Seen?

- ▶ In TogetherCC: UML class diagrams (annotated with OCL)
- ▶ In Eclipse: Java code annotated with JML
- ▶ Generation of proof obligations (POs) from Eclipse (or TogetherCC) + starting the KeY prover from Eclipse (or TogetherCC)
- ▶ Within the KeY prover:
  - ▶ POs rendered in JavaDL sequents
  - ▶ Construction + presentation of sequent proofs
  - ▶ (how to use the prover, really)
  - ▶ (design of the calculus)
  - ▶ ("taclet" language for defining rules)
  - ▶ (automation, implementation, ...)
- ▶ (how far does this carry us)

## Outline of our Tutorial

- ▶ Part I (you are here)
  - ▶ Intro
  - ▶ First Demo
  - ▶ Dynamic Logic intro
  - ▶ Specification: JML (+ UML/OCL)
  - ▶ Proof obligations
  - ▶ Integration in standard tools
  - ▶ [Second Demo](#)
- ▶ Part II
  - ▶ JavaCardDL: the *logic*
  - ▶ Sequent Calculus
  - ▶ Symbolic execution
  - ▶ Design of the JavaCardDL *calculus* ([demos](#))

## Outline of our Tutorial (contd.)

- ▶ Part III
  - ▶ The “taclet” language and framework
  - ▶ Induction ([demo](#))
  - ▶ Arithmetic ([demo](#))
  - ▶ Automation
- ▶ Part IV
  - ▶ Interaction with the Prover ([demo](#))
  - ▶ Case studies

## The Logic: Dynamic Logic for Java

### Dynamic Logic (DL)

- ▶ Each FOL formula is a DL formula
- ▶ If  $\phi$  a DL formula and  $\alpha$  a program:
  - ▶  $\langle \alpha \rangle \phi$  is a DL formula
  - ▶  $[\alpha] \phi$  is a DL-Formula
- ▶ DL formulas are closed under FOL operators and connectives

Modalities can be arbitrarily nested

### Dynamic Logic for Java (JavaDL)

- ▶ In  $\langle \alpha \rangle \phi$ , and  $[\alpha] \phi$ ,  $\alpha$  is a list of **Java statements**
- ▶ *No encoding of programs*

## Meaning of Dynamic Logic Formulas

For deterministic programs (like single threaded Java):

- ▶  $\langle \alpha \rangle \phi$  :  $p$  terminates and  $\phi$  holds in the final state  
(total correctness)
- ▶  $[\alpha] \phi$  : If  $p$  terminates, then  $\phi$  holds in the final state  
(partial correctness)

## Relation to Hoare Logic

### “Partial correctness” assertion

Hoare triple:

$$\{\psi\} \alpha \{\phi\}$$

“If  $\alpha$  is started in a state satisfying  $\psi$  and terminates, then its final state satisfies  $\phi$ .”

in DL

$$????\psi \rightarrow [\alpha]\phi$$

## JavaDL Examples

### Valid formulas

- ▶  $\langle x = 1; y = 3; \rangle x < y$
- ▶  $x < y \rightarrow \langle x++; \rangle x \leq y$
- ▶  $[\text{while}(\text{true})\{x = x;\}] \text{false}$

### Non-valid formulas

- ▶  $x < y \rightarrow \langle x = y; y = x; \rangle y < x$
- ▶  $x < y \rightarrow \langle x++; \rangle x < y$
- ▶  $[\text{while}(x \neq 0)\{x = x;\}] \text{false}$

## Alternative Formalisms for Correctness Assertions

### Correctness Assertions

Can be stated:

1. In the oo specification languages
  - ▶ **JML** (Java Modeling Language)
  - ▶ **OCL** (Object Constraint Language, part of UML)
2. In **JavaDL** directly

### Proof Obligations (POs)

Always in JavaDL,

Either generated from specifications (1.) and implementations, or “hand-crafted” (2.)

## Architectural Set Ups (1. – 4.)

### With “hand-crafted” POs

1. **KeY stand alone prover**, loading POs from .key files

### With automatic PO generation

- ▶ From JML and Java
  2. **JML browser + KeY stand alone prover**
  3. **Eclipse with KeY plug-in**
- ▶ From OCL/UML and Java
  4. **TogetherCC with KeY-extensions**

## Java Modeling Language (JML)

### A notation for formally specifying

- ▶ Behaviour of Java methods
- ▶ Admissible states of Java objects

### Important features

- ▶ Pre/post conditions and invariants
- ▶ Notational consistency with Java expressions  
(Java expressions allowed in JML expressions,  
including side effect free method calls)
- ▶ “Specification only” fields and methods
- ▶ Restricting scope of side effects

JML specs appear as comments in .java files

## JML example 1

```
/*@
  @ public normal_behavior
  @ requires   insertedCard != null;
  @ requires   !customerAuthenticated;
  @ requires   pin == insertedCard.correctPIN;
  @ ensures   customerAuthenticated;
  @ assignable customerAuthenticated;
  @*/
public void enterPIN (int pin) {
    if ....
```

## JML example 2

```
/*@ <example 1>
  @ also
  @
  @ public normal_behavior
  @ requires   insertedCard != null;
  @ requires   !customerAuthenticated;
  @ requires   pin != insertedCard.correctPIN;
  @ requires   wrongPINCounter < 2;
  @ ensures   wrongPINCounter == \old\old(wrongPINCounter) + 1;
  @ assignable wrongPINCounter;
  @*/
public void enterPIN (int pin) {
    if ....
```

## JML example 3

```
/*@ <example 1> also <example 2>
  @ also
  @
  @ public normal_behavior
  @ requires   insertedCard != null;
  @ requires   !customerAuthenticated;
  @ requires   pin != insertedCard.correctPIN;
  @ requires   wrongPINCounter >= 2;
  @ ensures   insertedCard == null;
  @ ensures   \old(insertedCard).invalid;
  @ assignable insertedCard, wrongPINCounter,
  @           insertedCard.invalid;
  @*/
public void enterPIN (int pin) {
    if ....
```

## JML example 4

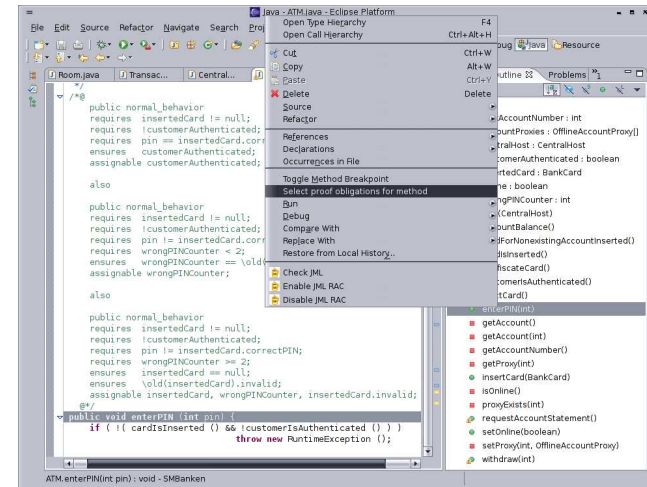
```
public class ATM {
/*@
 @ public invariant public invariant
 @     accountProxies != null; accountProxies != null;
 @ public invariant public invariant
 @     accountProxies.length == maxAccountNumber; accountProxies
 @ public invariant
 @     (\forall int i;
 @         i >= 0 && i < maxAccountNumber;
 @         ( accountProxies[i] == null
 @             ||
 @             accountProxies[i].accountNumber == i ));
 @*/
private /*@ spec_public @*/
    OfflineAccountProxy[] accountProxies =
        new OfflineAccountProxy [maxAccountNumber];
```

## Eclipse

- ▶ *The modern IDE for Java*
- ▶ Provides powerful coding support:
  - ▶ Code templates, code completion
  - ▶ Import management
- ▶ *Freely available* via [eclipse.org](http://eclipse.org)
- ▶ Very popular and widely distributed
- ▶ Well documented plug-in interface

## KeY-Eclipse integration

Eclipse context menus, like:



Trigger generation of selected POs + launch prover window

## Generating Proof Obligations

- ▶ JML expressions  $e$  automatically translated into formula  $\mathcal{T}(e)$  (in simple cases FOL, in general JavaDL)
- ▶ Java is *not* translated, calculus works on unaltered source code
- ▶ Both combined in JavaDL

## Proof Obligations: Postconditions

### Given:

- ▶ Implementation  $\alpha$  of method  $m$  of class  $C$
- ▶ JML 'requires'  $P$  for  $m$
- ▶ JML 'ensures'  $Q$  for  $m$
- ▶ JML declares 'invariant'  $I$  for  $C$

### Prove:

- ▶  $T(I) \& T(P) \rightarrow \langle \alpha \rangle T(Q)$

$T(expr)$  = translation of the JML expression  $expr$  into DL

## Proof Obligations: Invariants

### Given:

- ▶ Implementation  $\alpha$  of method  $m$  of class  $C$
- ▶ JML **invariant**  $I$  of  $C$
- ▶ JML precondition  $P$  of  $m$

### Prove:

- ▶  $T(P) \& T(I) \rightarrow \langle \alpha \rangle T(I)$

## Alternative to JML: OCL/UML

### Unified Modeling Language — UML

*Visual* language for OO modelling  
Standard of Object Management Group (OMG)  
Best-known feature: class diagrams

### Object Constraint Language — OCL

*Textual* specification language  
UML sub-standard  
Pre/post condition and invariants, attached to class diagrams

## KeY-TogetherCC Integration

### TogetherCC

Commercial case tool (Borland), supporting UML

### KeY extends TogetherCC by:

- ▶ Authoring support for OCL constraints  
OCL – natural language translation and co-editing
- ▶ PO generation from TogetherCC context menus
- ▶ Launching the KeY prover from TogetherCC context menus

## JavaCard

Main target application: **smart cards**

- ▶ Relative small applications
- ▶ Often security/financially/legally critical

KeY system supports a smart card version of Java: **JavaCard**

## JavaCard vs. Java

### Features omitted in JavaCard

- ▶ Multi threading
- ▶ Floating point types
- ▶ Garbage collection (implementation optional)
- ▶ Dynamic class loading

### Additional feature of JavaCard

- ▶ Transaction mechanism

## JavaCard

KeY supports

**100% JavaCard**

## Second Demo



## After the Break

- ▶ Part I
  - ▶ Intro
  - ▶ First Demo
  - ▶ Java Dynamic Logic intro
  - ▶ Specification: JML (+ UML/OCL)
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  - ▶ Integration in standard tools
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  - ▶ JavaCardDL: the *logic*
  - ▶ Sequent Calculus
  - ▶ Symbolic execution
  - ▶ Design of the JavaCardDL *calculus* (demos)

## Part II Logic and Calculus

## Dynamic Logic Syntax

A first-order program logic for modeling change of computation states

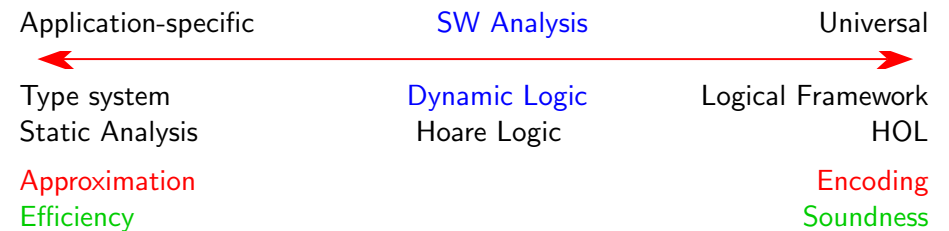
```
ProgramFormula ::=  
    FOFormula |  
    TotalCorrectnessModality ProgramFormula |  
    PartialCorrectnessModality ProgramFormula
```

```
TotalCorrectnessModality ::= '<' CompilableJavaCardStatement '>'
```

```
PartialCorrectnessModality ::= '[' CompilableJavaCardStatement ']'
```

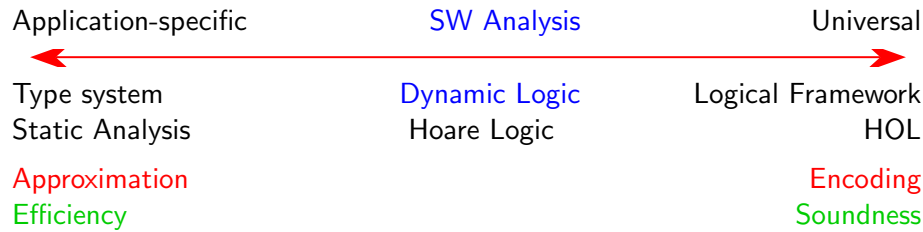
- ▶ Modal formulas closed under logical operations (cf. Hoare logic)
- ▶ JavaCardDL formulas contain unaltered JavaCard source code

## Why Dynamic Logic?





## Why Dynamic Logic?



► Proven technology that scales up

- Used in verification systems KIV, VSE since 1986
- Massive case studies involving imperative programs

## Some JavaCardDL Syntax Issues

- FO logical variables disjoint from program variables
  - No quantification over program variables
  - Programs contain no logical variables
- ASCII syntax, key words preceded ‘\’
- Usual precedence, add brackets where necessary
- If program p appears in a DL formula then the class definitions of all types referenced in p are assumed to be present as well

## Dynamic Logic Semantics I

Program formulas evaluated relative to **computation state s** and **variable assignment β**

### Example

$\backslash \text{forall } \textit{int } x; (\langle \textit{int } i = j++; \rangle (i = x))$

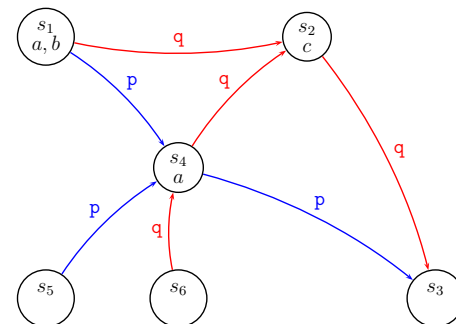
### Definition

$s, \beta \models \langle p \rangle \phi$  iff p **totally correct** wrt s and β iff p started in s terminates normally and  $s', \beta \models \phi$  in final state s' after execution of p

$s, \beta \models [p] \phi$  iff p **partially correct** wrt s and β iff whenever started in s p terminates normally then in s',  $\beta \models \phi$  final state s' after execution of p  
(We rely on Java programs being deterministic)

## Dynamic Logic Semantics Example

Kripke structure, where worlds are computation states  
Boolean program variables a, b, c, programs p, q



$s_1 \models \langle p \rangle a$  ?(ok)    $s_1 \models \langle q \rangle a$  ?(-)    $s_5 \models \langle q \rangle a$  ?(-)    $s_5 \models [q] a$  ?(ok)

## First-Order Formula Syntax

FOFormula ::= TernaryOpFormula | BinaryOpFormula |  
UnaryOpFormula | NullaryOpFormula |  
QuantifiedFormula | AtomicFormula

TernaryOpFormula ::=  
`\if ( ' FOFormula ' ) \then ( ' FOFormula ' ) \else ( ' FOFormula ' )`

BinaryOpFormula ::= FOFormula BinaryOp FOFormula

BinaryOp ::= '&' | '|' | '→' | '↔'

UnaryOpFormula ::= '! FOFormula

NullaryOpFormula ::= 'true' | 'false'

QuantifiedFormula ::= Quantifier Type LogVar ';' FOFormula

Quantifier ::= '\forall' | '\exists'

## Dynamic Logic Example Formulas

`\forall int y; ((⟨x = 1;⟩ x = y) ↔ (⟨x = 1*1;⟩ x = y))` **Syntax ?**  
ok

`\exists int x; ([x = 1;](x = 1))` **Syntax ? bad**

- ▶ x cannot be **logical variable**, because it occurs in program
- ▶ x cannot be **program variable**, because it is quantified

`⟨x = 1;⟩([while (true) {}] false)` **Syntax ? ok**

- ▶ Program formulas can appear nested

`⟨int x;⟩\forall int y; ((⟨p⟩ x = y) ↔ (⟨q⟩ x = y))` **ok**

- ▶ p, q **equivalent** relative to computation state restricted to x

## First-Order Term Syntax

Terms are statically typed like in Java

- ▶ **Type** is partially ordered finite set of type symbols  $\{t_1, \dots, t_r\}$  closed under  $\sqcap$ , contains Java types
- ▶ Each logical variable  $x \in \text{LogVar}$  has **static type**  $t$ , declared  $t \ x$
- ▶  $x$  is term of type  $t$  for variable declared as  $t \ x$
- ▶ Function symbols and predicate symbols declared with **signature**
  - ▶ Type FunctionSymbol [ '( Type {',' Type }\* ' ) ]
  - ▶ PredicateSymbol [ '(Type {',' Type }\* ' ) ]
- ▶ Arguments of complex terms must **conform to** (in the sense of Java) type declared in their signature
- ▶ **Equality** symbol '=' for most argument types
- ▶ Otherwise **no overloading** of variables, functions, predicates

## Type System Semantics

Type system semantics accounts for dynamic types of terms

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Type system semantics accounts for dynamic types of terms

- ▶ **Universe**  $U$  disjoint union of subuniverses  $U^t$  for each type  $t$

- ▶ Type  $t$  interpreted in the (possibly empty) subuniverse  $U^t$
- ▶ Not all subuniverses  $U^t$  are populated (allow abstract classes)

## Type System Semantics

Type system semantics accounts for dynamic types of terms

- ▶ Let  $T(t) = \bigcup_{t_0 \prec t} U^{t_0}$  be the universe elements **typeable** with  $t$

Each  $T(t)$  contains typable objects, at least `null`

## Type System Semantics

Type system semantics accounts for dynamic types of terms

- ▶ Each term has **static type** (declared type of outermost symbol)

## Type System Semantics

Type system semantics accounts for dynamic types of terms

- ▶ The **dynamic** (runtime) type of a term  $e$  is **the**  $t$  such that  $e \in U^t$

Dynamic type of  $e$  always conforms to its static type

## Type System Semantics

Type system semantics accounts for dynamic types of terms

- ▶ Check dynamic type with **type function**: `Type::instance('Term')`

## Rigid and Flexible Terms in Dynamic Logic

Certain FO terms correspond to Java locations:  
**program variables, array access, attribute access**

### Example

```
⟨int i;⟩\forall int x;(i + 1 = x -> ⟨i++;⟩(i = x))
```

- ▶ Interpretation of **i** depends on computation state ⇒ **flexible**

Locations are always interpreted flexible

## Rigid and Flexible Terms in Dynamic Logic

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### Example

```
⟨int i;⟩\forall int x;(i + 1 = x -> ⟨i++;⟩(i = x))
```

## Rigid and Flexible Terms in Dynamic Logic

Certain FO terms correspond to Java locations:  
**program variables, array access, attribute access**

### Example

```
⟨int i;⟩\forall int x;(i + 1 = x -> ⟨i++;⟩(i = x))
```

- ▶ Interpretation of **x** and **+** **must not** depend on state ⇒ **rigid**

Logical variables, standard library functions declared rigid

A term containing at least one flexible symbol is flexible, otherwise rigid

## Kripke Semantics

## Kripke Semantics

- ▶  $U$  is fixed: all objects with dynamic type  $t$  are in  $U^t$  from beginning

Objects have attributes  $o.<created>$  and  $o.<initialized>$   
These are set appropriately during object creation

## Kripke Semantics

## Kripke Semantics

- ▶ States  $s = (U, I_s) \in S$  have typed universe  $U$ , FO interpretation  $I_s$

$I_s$  interprets rigid symbols identically in each state

- ▶ Semantics of Java program  $p$  is **partial function**  $\rho(p) : S \rightarrow S$

$s, \beta \models \langle p \rangle \phi$  iff  $\rho(p)(s) \downarrow$  and  $\rho(p)(s), \beta \models \phi$

# Kripke Semantics

- ▶ A JavaCardDL formula  $\phi$  is **valid** iff  $s, \beta \models \phi$  for all  $\beta$  and all  $s$

Quantification over **all** computation states

# State Update Semantics

Need to define  $\rho$  for each program  $p$  — start with **assignment**

## Definition

**State update** of  $I$  at  $t$   $x$  with  $u \in T(t)$

$$I_x^u(y) = \begin{cases} I(y) & x \neq y \\ u & x = y \end{cases}$$

**Assignment semantics** is state update:

$$\rho(x=e;)(I) = I_x^{e.I, \beta}$$

- ▶  $e$  must be side effect-free, no reference type
- ▶ Identify states with interpretation since  $U$  is fixed

# Program Semantics

In general,  $\rho(p)$  defines operational semantics for  $p$

- ▶  $\rho(\text{if } (b) \{ \alpha \} \text{ else } \{ \gamma \};)(I) = \begin{cases} \rho(\alpha)(I) & I, \beta \models b = \text{TRUE} \\ \rho(\gamma)(I) & \text{otherwise} \end{cases}$
- ▶  $\rho(\text{while } (b) \{ \alpha \};)(I) = I'$  iff there are  $I = I_0, \dots, I_n = I'$  such that
  - ▶  $I_j, \beta \models b = \text{TRUE}$  for  $0 \leq j < n$
  - ▶  $\rho(\alpha)(I_j) = I_{j+1}$  for  $0 \leq j < n$
  - ▶  $I_n, \beta \models b = \text{FALSE}$  undefined otherwise

Problems:

- ▶ Definitions work only under simplistic assumptions:
  - b side-effect free, no exceptions, no breaks, ...
- ▶ We need a calculus (syntactic characterization)

Develop a calculus for JavaCard that directly realizes an operational semantics with adequate syntactic means

# Sequents and their Semantics

Sequent ::= [FormulaList] '==>' [FormulaList]

FormulaList ::= ProgramFormula {',' ProgramFormula}\*

## Notation

$$\underbrace{\psi_1, \dots, \psi_m}_{\text{Antecedent}} \implies \underbrace{\phi_1, \dots, \phi_n}_{\text{Succedent}}$$

Schema variables  $\phi, \psi$  match program formulas

Schema variables  $\Gamma/\Delta$  match sublists of antecedent/succedent

## Semantics

same as **formula** of sequent:  $(\psi_1 \& \dots \& \psi_m) \rightarrow (\phi_1 | \dots | \phi_n)$

(No free logical variables occur in program formulas)



## Sequent Rules

$$\text{RULE NAME} \frac{\overbrace{\Gamma_1 \implies \Delta_1 \quad \dots \quad \Gamma_r \implies \Delta_r}^{\text{Premises}}}{\underbrace{\Gamma \implies \Delta}_{\text{Conclusion}}}$$

**Sound** rule (essential):

$$\models (\text{fml}(\Gamma_1 \implies \Delta_1) \ \& \ \dots \ \& \ \text{fml}(\Gamma_r \implies \Delta_r)) \ \rightarrow \ \text{fml}(\Gamma \implies \Delta)$$

**Complete** rule (desirable):

$$\models \text{fml}(\Gamma \implies \Delta) \ \rightarrow \ (\text{fml}(\Gamma_1 \implies \Delta_1) \ \& \ \dots \ \& \ \text{fml}(\Gamma_r \implies \Delta_r))$$

Admissible to have no premisses (iff conclusion is valid: **axiom**)

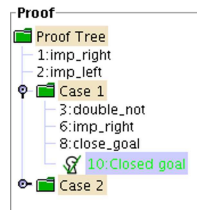
## Sequent Calculus Proofs

**Goal** to prove validity of:  $\mathcal{G} = \psi_1, \dots, \psi_m \implies \phi_1, \dots, \phi_n$

- ▶ find rule  $\mathcal{R}$  whose conclusion matches  $\mathcal{G}$
- ▶ instantiate  $\mathcal{R}$  such that conclusion identical to  $\mathcal{G}$
- ▶ check that side conditions of  $\mathcal{R}$  are satisfied
- ▶ mark  $\mathcal{G}$  as closed if  $\mathcal{R}$  was axiom
- ▶ recursively find proofs for resulting premisses  $\mathcal{G}_1, \dots, \mathcal{G}_r$
- ▶ tree structure with goal sequent as root
- ▶ proof is finished when all goals are closed

### Goal-directed proof search

In KeY tool proof displayed as JAVA Swing tree



## Some Simple Sequent Rules

$$\text{NOT\_LEFT} \frac{\Gamma \implies A, \Delta}{\Gamma, !A \implies \Delta}$$

$$\text{IMP\_LEFT} \frac{\Gamma \implies A, \Delta \quad \Gamma, B \implies \Delta}{\Gamma, A \rightarrow B \implies \Delta}$$

$$\text{CLOSE\_GOAL} \frac{}{\Gamma, A \implies A, \Delta} \quad \text{CLOSE\_BY\_TRUE} \frac{}{\Gamma \implies \text{true}, \Delta}$$

$$\text{ALL\_LEFT} \frac{\Gamma, \forall \text{forall } t \ x; \phi, \{x/e^{t'}\}\phi \implies \Delta}{\Gamma, \forall \text{forall } t \ x; \phi \implies \Delta}$$

$e^{t'}$  var-free term of type  $t' < t$

## Proof by Symbolic Program Execution

Which sequent rules for program formulas?  
What corresponds to top-level connective in **sequential** program?

**First executable statement:** follow natural program control flow

Sound and complete rule for conclusions with main formulas:

$$\langle p; \omega \rangle \phi, \quad [p; \omega] \phi$$

where  $p$ ; single legal Java statement,  $\omega$  the remaining program

Sequent rules **execute symbolically** the first active statement  
Sequent proof corresponds to **symbolic program execution**

## A Naive Rule for Assignment

$$\text{ASSIGNMENT} \frac{\{x/x_{old}\}\Gamma, x = \{x/x_{old}\}e \implies \langle\omega\rangle\phi, \{x/x_{old}\}\Delta}{\Gamma \implies \langle x = e; \omega \rangle \phi, \Delta}$$

$x_{old}$  new program variable that “rescues” old value of  $x$

### Problems

- ▶ **Renaming** makes it difficult to keep track of computation state
- ▶ Does not work when  $e$  has **side effects** or when  $x$  is not variable
- ▶ Does not work for **reference types**
- ▶ **“Eager”** rule: bad if state change at  $x$  is cancelled out by later assignment or is irrelevant for  $\phi$

## Specifying Initial Values

How to express correctness for arbitrary **initial** value of program variable?  
Cannot quantify over program variables!

**Not allowed:**  $\forall \text{forall } \text{int } i; \langle p(\dots i \dots) \rangle \phi$   
(program  $\neq$  logical variable)

**Not intended:**  $\implies \langle p(\dots i \dots) \rangle \phi$  (Validity of sequents:  
quantification over *all* states)

**Not allowed:**  $\forall \text{forall } \text{int } n; \langle p(\dots n \dots) \rangle \phi$   
(no logical variables in programs)

### Solution

Use explicit construct to record state change information

**(State) update**  $\forall \text{forall } \text{int } n; (\{i := n\} \langle p(\dots i \dots) \rangle \phi)$

## Explicit State Updates

**Updates** record state change

**Syntax**( $v$ ,  $e$  have value types,  $e$  conforms to  $v$ )

If  $v$  is program variable,  $e, e'$  FO terms, and  $\phi$  any DL formula, then  $\{v := e\}\phi$  is DL formula and  $\{v := e\}e'$  is FO term

### Semantics

$I, \beta \models \{v := e\}\phi$  iff  $I_{\beta}^{e, \beta}, \beta \models \phi$

Semantics identical to that of assignment

**Updates** work like “lazy” assignments

- ▶ Updates are **not assignments**: may contain logical variables
- ▶ Updates are **not equations**: change interpretation of PVs

## Computing the Effect of Updates

The simplest case:  $x$  program variable with **value type**

## Computing the Effect of Updates

The simplest case:  $x$  program variable with **value type**

Apply update to **program variable**

$$\begin{aligned}\{x := e\}y &\rightsquigarrow y \\ \{x := e\}x &\rightsquigarrow e\end{aligned}$$

## Computing the Effect of Updates

The simplest case:  $x$  program variable with **value type**

Apply update to **logical variable**

$$\{x := e\}w \rightsquigarrow w$$

## Computing the Effect of Updates

The simplest case:  $x$  program variable with **value type**

Apply update to **complex term**

$$\{x := e\}f(e_1, \dots, e_n) \rightsquigarrow f(\{x := e\}e_1, \dots, \{x := e\}e_n)$$

Similar for FOL formulas (like [substitution](#))

Update followed by **program formula**

$$\{x := e\}(\langle p \rangle \phi) \rightsquigarrow \{x := e\}(\langle p \rangle \phi) \quad \text{unchanged!}$$

Update computation delayed until  $p$  symbolically executed

## Composition of Updates

Updates **lazily** applied (delayed until “final” state), but **eagerly** simplified

Applying updates to updates: **composition** of states

$$\{l_1 := r_1\}\{l_2 := r_2\} = \{l_1 := r_1, l_2 := \{l_1 := r_1\}r_2\}$$

Results in **parallel update**:  $\{l_1 := v_1, \dots, l_n := v_n\}$

**Semantics**

- ▶ All  $l_i$  and  $v_i$  computed in old state
- ▶ All updates done simultaneously
- ▶ On conflict  $l_i = l_j, v_i \neq v_j$  **last update wins**

For example,  $\{i := 1 + 2, i := 2\} \rightsquigarrow \{i := 2\}$

## Assignment Rule Revisited

$$\text{ASSIGN} \frac{\Gamma \Longrightarrow \{x := e\} \phi, \Delta}{\Gamma \Longrightarrow \langle x = e; \rangle \phi, \Delta}$$

Rules dealing with programs need to account for updates

Notational convention:

- ▶ Updates already present in conclusion not displayed explicitly
- ▶ New updates in premise inserted after last present update

Updates simplified eagerly!

Demo: `rh.assign.key`

## Some Non-Trivial Java Features

Illustrate main ideas in JavaCardDL calculus

- ▶ **Complex** expressions with **side effects**  
`int i = 0; if ((i=2) >= 2) {i++;} // value of i?`
- ▶ **Exceptions** (try-catch-finally)
- ▶ **Aliasing**  
Different navigation expressions may be same object reference

$$I \models o.\text{age} \doteq 1 \rightarrow \langle u.\text{age} = 2; \rangle o.\text{age} \doteq u.\text{age} \quad ?$$

Depends on whether  $I \models o \doteq u$

## The Design Space of a Calculus

All JavaCard language features are fully addressed in KeY

Be aware of the full design space!

## The Design Space of a Calculus

All JavaCard language features are fully addressed in KeY

Be aware of the full design space!

- ▶ Program transformation, up-front

**Pro:** Feature needs not be handled in calculus

**Contra:** Soundness, modified source code

**Example in KeY:** Only a few rare features, for example, inner classes

## The Design Space of a Calculus

All JavaCard language features are fully addressed in KeY

Be aware of the full design space!

- ▶ Local transformation, done by a rule on-the-fly

**Pro:** Flexible, easy to implement, usable, less rules needed

**Contra:** Not expressive enough for all features

**Example in KeY:** Complex expressions, method expansion (many others)

## The Design Space of a Calculus

All JavaCard language features are fully addressed in KeY

Be aware of the full design space!

- ▶ Special purpose constructs in program logic

**Pro:** Arbitrarily expressive extensions possible

**Contra:** Increases complexity of all rules

**Example in KeY:** Abrupt termination, method call, updates, blocks

## The Design Space of a Calculus

All JavaCard language features are fully addressed in KeY

Be aware of the full design space!

- ▶ Modeling with first-order formulas

**Pro:** No extension required, enough to express most features

**Contra:** Creates difficult FO POs, unreadable antecedents, too eager

**Example in KeY:** Dynamic types, branch predicates

## Highlights from JavaCardDL

Expressions with Side Effects

**Local program transformation** ensures side effect-free expressions

Compute complex subexpressions separately and store in temp. variable

```
i = j++;                                int var = j;
                                         j = (int)(j+1);
                                         i = var;
```

Require guards in all rules to be **simple expressions**

$$\text{IF-SPLIT} \frac{\Gamma, \mathbf{b} \doteq \text{TRUE} \implies \langle \pi \mathbf{p} \omega \rangle \phi, \Delta \quad \Gamma, \mathbf{b} \doteq \text{FALSE} \implies \langle \pi \omega \rangle \phi, \Delta}{\Gamma \implies \langle \pi \text{if } (\mathbf{b}) \{ \mathbf{p} \}; \omega \rangle \phi, \Delta}$$

Demo: rh\_post\_incr.key

# Highlights from JavaCardDL

## Abrupt Termination

Redirection of control flow via **exceptions**

$$\langle \pi \text{ try } \{pq\} \text{ catch}(T \ e) \{r\} \text{ finally } \{s\}; \omega \rangle \phi$$

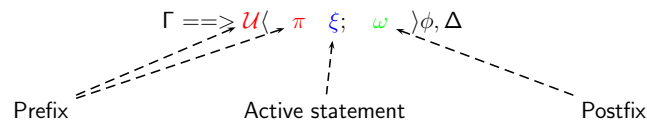
# Highlights from JavaCardDL

## Abrupt Termination

Redirection of control flow via **exceptions**

$$\langle \pi \text{ try } \{pq\} \text{ catch}(T \ e) \{r\} \text{ finally } \{s\}; \omega \rangle \phi$$

Solution: symbolic execution rules work on **first active statement** after **prefix**, followed by **postfix**



# Highlights from JavaCardDL

## Try-throw // Symbolic execution

Catching a **throw** statement is controlled by **prefix** and **postfix**

TRY-THROW (exc simple)

$$\frac{\Gamma \implies \left\langle \begin{array}{l} \pi \text{ if (exc instanceof T)} \\ \{ \text{try } \{e=\text{exc}; r\} \text{ finally } \{s\} \} \\ \text{else } \{s \text{ throw exc}; \omega \} \end{array} \right\rangle \phi}{\Gamma \implies \langle \pi \text{ try } \{ \text{throw exc}; q \} \text{ catch}(T \ e) \{r\} \text{ finally } \{s\}; \omega \rangle \phi}$$

Demo: rh\_exc.key

## Symbolic Execution

**Symbolic:** Only static information available, proof splitting

**Execution:** Runtime infrastructure required in calculus

# Highlights from JavaCardDL

## Aliasing

Naive alias resolution causes **proof split** at each reference type access

$$\Gamma, o.\text{age} \doteq 1 \implies \langle \pi \ u.\text{age} = 2; \omega \rangle o.\text{age} \doteq u.\text{age}$$

Unnecessary in many cases!

$$\Gamma, o.\text{age} \doteq 1 \implies \langle \pi \ u.\text{age} = 2; \ o.\text{age} = 2; \omega \rangle o.\text{age} \doteq u.\text{age}$$

$$\Gamma \implies \langle \pi \ o.\text{age} = 1; \ u.\text{age} = 2; \omega \rangle u.\text{age} \doteq 2$$

**Updates** avoid such proof splits:

- **Delay** application of state computation after program execution
- **Eager** simplification of updates, accumulate effect

Simplification and application of updates with reference types not trivial!

Demo: rh\_alias.key

## After the Break

But how does this work in practice?

- ▶ How are rules implemented?
- ▶ How “automatic” are they applied?
- ▶ What about Java integer types?
- ▶ And loops? How does induction work?
- ▶ How does the prover interface support its user?

**Stay tuned to KeY 1.0 !**

### Part III

## The Prover: Concepts, Implementation, Automation

## Taclets and Taclet Language

### Taclets

Taclets ...

- ▶ have logical content like rules of the calculus.
- ▶ have pragmatic information for interactive application.
- ▶ have pragmatic information for automated application.
- ▶ keep all these concerns separate but close to each other.
- ▶ can easily be added to the system.
- ▶ are given in a textual format.
- ▶ can be “validated” w.r.t. more primitive taclets.

## Taclet Syntax

Consider a “modus ponens” rule:

$$\frac{\Gamma, \phi, \psi \implies \Delta}{\Gamma, \phi, \phi \rightarrow \psi \implies \Delta}$$

Here it is as a taclet:

```
\find (b -> c ==>) \assumes (b ==>) \replacewith(c ==>)\heuristics(simplify)
```

- ▶ schema variables
- ▶ turnstile ( $\vdash$ )
- ▶ find clause
- ▶ action clause
- ▶ assumes clause
- ▶ heuristic declaration

## A Branching Rule

```
close_goal {
  \assumes (b ==>) \find (==> b)
  \closegoal
  \heuristics(closure)
};
```

```
???cut {
  \add (b ==>); \add (==> b)
};
```

## “The Small Print”

Consider the rule for existential quantifiers:

$$\frac{\Gamma, \phi(f(x_1, \dots, x_n)) \implies \Delta}{\Gamma, \exists x; \phi(x) \implies \Delta}$$

where  $x_1, \dots, x_n$  are the free variables occurring in  $\phi(x)$  and  $f$  is a new function symbol with static type  $t$ .

```
ex_left {
  \find (\exists u; b ==>)
  \varcond ( \new(sk, \dependingOn(b)) )
  \replacewith ({\subst u; sk}b ==>)
  \heuristics (delta)
};
```

```
\new(v), \notFreeIn(x,y),
\isLocalVariable(v), \static(v), ...
```

## Java Card Taclets

Rule `if_else_split`

$$\frac{\Gamma, B \doteq \text{true} \implies \langle \dots \alpha_1; \dots \rangle F, \Delta \quad \Gamma, B \doteq \text{false} \implies \langle \dots \alpha_2; \dots \rangle F, \Delta}{\Gamma \implies \langle \dots \text{if } (B) \alpha_1 \text{ else } \alpha_2; \dots \rangle F, \Delta}$$

with  $B$  a Boolean expression without side effects

Corresponding taclet

```
if_else_split {
  \find (==> <{.. if(#se) #s0 else #s1 ...}>post)
  \replacewith (==> <{.. #s0 ...}>post) \add (#se = TRUE ==>);
  \replacewith (==> <{.. #s1 ...}>post) \add (#se = FALSE ==>)
  \heuristics(if_split)
};
```



## Soundness

### “Higher order skolemization”

Modus ponens:

$$\frac{\Gamma, \phi, \psi \implies \Delta}{\Gamma, \phi, \phi \rightarrow \psi \implies \Delta}$$

Validation proof obligation:

$$\backslash\text{forall } \phi; \backslash\text{forall } \psi; ((\phi \rightarrow \psi) \ \& \ \phi) \rightarrow \psi$$

After skolemization:

$$((p \rightarrow q) \ \& \ p) \rightarrow q$$

### Cross-checking against other Java semantics

- ▶ Bali
- ▶ Java semantics in Maude

## Summary

Taclets ...

- ▶ simple and powerful
- ▶ compact and clear notation
- ▶ no complicated meta-language
- ▶ easy to apply with a GUI
- ▶ validation possible

## Integer Arithmetics

## Data Type Gap

### Specification Level

- ▶ Abstract data types
- ▶ Integer ( $\mathbb{Z}$ ), Set, List

### Implementation Level

- ▶ Concrete programming language data types
- ▶ byte, short, int, long, Array

# Data Type Gap: Integer Semantics

## OCL type Integer

- ▶ Infinite range, operators have usual mathematical semantics ( $\mathbb{Z}$ )

## Java types byte, short, int, long

- ▶ Different finite ranges
- ▶ Semantics of operators as in  $\mathbb{Z}$  except that:

**overflow occurs if result exceeds range,  
i.e., result is calculated modulo size of data type.**

- ▶ Overflow occurs silently

# More Formal Semantics of Java Integer Types

## Range of primitive integer types in Java

Type	Range	Bits
byte	$[-128, 127]$	8
short	$[-32768, 32767]$	16
int	$[-2147483648, 2147483647]$	32
long	$[-2^{63}, 2^{63} - 1]$	64

# Examples

## Valid for Java integer semantics

$MAX\_INT+1 = MIN\_INT$   
 $MIN\_INT*(-1) = MIN\_INT$   
 $\exists int\ x, y; !x = 0 \ \& \ !y = 0 \ \& \ x*y = 0$

## Not valid for Java integer semantics

$\forall int\ x; \exists int\ y; y > x$

## Not a sound rewrite rules for Java integer semantics

$x+1 > y+1 \rightsquigarrow x > y$

# General Problem revisited

- ▶ Semantic gap between  $\mathbb{Z}$  and Java integers
- ▶ Defining a JavaDL semantics for Java integers that...
  - ▶ is a correct data refinement of  $\mathbb{Z}$  Req. (Z)
  - ▶ reflects Java integer semantics Req. (J)

## 3 possible approaches

Semantics	Description	Req. (Z)	Req. (J)
$S_{OCL}$	corresponds to semantics of $\mathbb{Z}$	✓	✗
$S_{Java}$	corresponds to Java semantics	✗	✓
$S_{KeY}$	hybrid of $S_{OCL}$ and $S_{Java}$	✓	✓

## Semantics $\mathcal{S}_{OCL}$

$\mathcal{S}_{OCL}$  assigns Java integers the semantics of  $\mathbb{Z}$

- ▶ Req. (Z) trivially fulfilled
- ▶ Req. (J) violated, incorrect programs can be “verified”

Example:

$\models_{\mathcal{S}_{OCL}} \langle y=x+1; \rangle y = x +_{\mathbb{Z}} 1$

but for  $x = \text{MAX\_INT}$  program not correct

## Semantics $\mathcal{S}_{Java}$

$\mathcal{S}_{Java}$  assigns Java integers the semantics defined in the JLS

- ▶ Req. (Z) violated  
several abstract states mapped onto one concrete state
- ▶ Req. (J) trivially fulfilled

No incorrect programs can be verified, **but**

- ▶ Existence of “incidentally” correct programs
- ▶ Difficult to reason about

## Our Approach: Semantics $\mathcal{S}_{KeY}$

1. Show the program correct for  $\mathbb{Z}$
2. Show that no overflow occurs at every step

---

Program correct w.r.t. Java semantics

## A Sequent Calculus For $\mathcal{S}_{KeY}$

Example: Rule for addition  
generates conditions that no overflow occurs  
with help of predicate  $in_T(x) \equiv \text{MIN}_T \leq x \leq \text{MAX}_T$

$$\frac{\begin{array}{l} (1) \Gamma \implies \{z := x + y\} \langle \rangle \phi \\ (2) \Gamma, in_T(x), in_T(y) \implies in_T(x + y), \langle z=x+y; \rangle \phi \end{array}}{\Gamma \implies \langle z=x+y; \rangle \phi}$$

## Summary

The KeY system has 3 pluggable integer semantics, of which  $\mathcal{S}_{KeY}$  has the best properties:

- ▶ Safe (though slight loss of completeness)
- ▶ Familiar reasoning
- ▶ Modularized proofs
- ▶ Proof reuse possible when switching from other semantics

## Proving Loops with Induction

## Basic Integer Induction Rule

$$\frac{\begin{array}{l} (1) \Gamma \implies IH(0), \Delta \\ (2) \Gamma \implies \forall \text{forall } int \ i; (i \geq 0 \& IH(i) \rightarrow IH(i + 1)), \Delta \\ (3) \Gamma, \forall \text{forall } int \ i; (i \geq 0 \rightarrow IH(i)) \implies \Delta \end{array}}{\Gamma \implies \Delta}$$

$IH$  = induction hypothesis

$i$  = induction variable

## An Example

To be proven:

$\forall \text{forall } int \ n!; (n! > 0 \& i = 0 \rightarrow \{n := n!\} \langle \text{while } (i < n) \ i++; \rangle i \geq n)$

To be proven (after skolemization):

$n!_0 > 0 \& i = 0 \rightarrow \{n := n!_0\} \langle \text{while } (i < n) \ i++; \rangle i \geq n$

Induction hypothesis:

$\{n := n!_0\} \{i := n - k\} \langle \text{while } (i < n) \ i++; \rangle i \geq n$

Induction variable:  $k$

# Induction Obligations

**Base case** ( $k = 0$ )

$$\{n := n_0\}\{i := n - 0\}\langle\text{while } (i < n) \text{ } i++; \rangle i \geq n$$

**Step case** ( $k \rightsquigarrow k + 1$ )

$$\begin{aligned} &\{n := n_0\}\{i := n - k_1\}\langle\text{while } (i < n) \text{ } i++; \rangle i \geq n \rightarrow \\ &\{n := n_0\}\{i := n - (k_1 + 1)\}\langle\text{while } (i < n) \text{ } i++; \rangle i \geq n \end{aligned}$$

## Automation

## Summary

Induction . . .

- ▶ programs can be proved with the “basic” integer induction rule
- ▶ lots of human interaction necessary
- ▶ quite a viscous task
- ▶ research in automation is underway
- ▶ invariant rule an alternative

## Means of Automation Implemented in KeY

- ▶ Global strategies for automatically applying rules in series
- ▶ Free-variable calculus for constructing witnesses for quantified formulas (non-destructive, proof-confluent calculus)
- ▶ Invocation of external theorem provers, decision procedures
  - ▶ Simplify (from ESC/Java)
  - ▶ ICS
  - ▶ Planned: Export to SMT-LIB format

## Strategies

### Responsible for selecting next proof expansion step for each goal

1. All possible expansion steps for a goal are computed
  - ▶ Steps described by:
    - Applied rule/taclet, position, values of schema variables
  - ▶ Information is cached in *RuleIndex* and updated when sequent is altered
2. For each possible rule application a *cost* value is computed
  - ▶ Integer value: Lower numbers → Preferred steps
  - ▶ Cost functions take into account for instance:
    - Kind of rule, unifications necessary, depth and context of position
  - ▶ Different strategies use different cost functions
3. Step with lowest costs is executed
  - ▶ Again caching: Priority queue for sorting expansion steps

**Procedure is iterated until no further rules are applicable or chosen maximum number of rule applications is reached**

## Strategies Currently Present in KeY

### Strategies optimized for symbolically executing programs

- ▶ Come in different flavours: With/Without unwinding loops, etc.
- ▶ Concentrate on eliminating program and simplifying sequents

### Strategy handling first-order logic

- ▶ Implements a complete first-order theorem prover
- ▶ But: Weak support for theories (particularly arithmetic)

### Implementation of Strategies

- ▶ Strategies are written Java, direct part of prover
- ▶ Creating new special-purpose strategies is easy
- ▶ Cost functions described using a library of *feature* functions and connectives

## Free-Variable Calculus

### Existential variables used to postpone instantiation

- ▶ In KeY called *metavariables*
- ▶ Mostly for universally quantified formulas in antecedent

### Constraints used to represent unification

- ▶ Formula constraints (conjunctions of equations) added when terms have to be substituted for metavariables

$$\frac{\text{true} \ll [X_0 \equiv 0], \text{ false} \ll [X_0 \equiv 1], \ \backslash\text{forall } \textit{int } x; x = 0 \implies}{X_0 = 0, \ \backslash\text{forall } \textit{int } x; x = 0 \implies}}{\backslash\text{forall } \textit{int } x; x = 0 \implies}$$

## Incremental Closure in Free-Variable Calculus

### Closing proofs by simultaneously closing its goals

- ▶ When applying taclets with `\closegoal`, involved constraints are collected for goal
- ▶ Proof can be closed if consistent closure constraints exist for all goals
- ▶ In KeY: Consistency of closure constraints is checked recursively, closure constraints for all subtrees of proof tree are cached

### Color codes in proof tree for status of goals and subtrees

black		no closing constraints exist
blue		closing constraints exist
green		goal is closed with a valid constraint (i.e. no restrictions)

## Free-Variable Calculus (2)

### Calculus is non-destructive and proof-confluent

- ▶ Unifiers are never directly applied to proof
- ▶ No backtracking necessary (but: interactive backtracking possible)
- ▶ Calculus is mostly useful for pure first-order logic, combination with theories and modal logic ongoing issue

## Interaction and Automation

For realistic programs: Fully-automated verification impossible

### Goal in KeY: Integrate automated and interactive proving

- ▶ All easy or obvious proof steps should be automated
- ▶ Sequents presented to user should be simplified as far as possible
- ▶ Primary steps that require interaction: induction, treatment of loops
- ▶ Taclets enable interactive rule application mostly using mouse

### Typical workflow when proving in KeY (and other interactive provers)

1. Prover runs automatically as far as possible
2. When prover stops user investigates situation and gives hints (makes some interactive steps)
3. Go to 1

## Part IV

### The Prover: Interaction and Guidance Case Studies

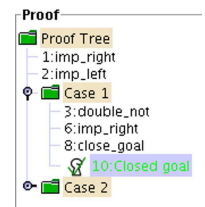
## Working with Proof Trees

### Displayed information

- ▶ Inner nodes labelled with rule that was applied
- ▶ Colors: **Green** signals closed subtrees  
**Blue** subtrees closed for suitable instantiation of metavariables

### Navigation

- ▶ By selecting inner nodes or leaves in tree
- ▶ By selecting leaves in goal list



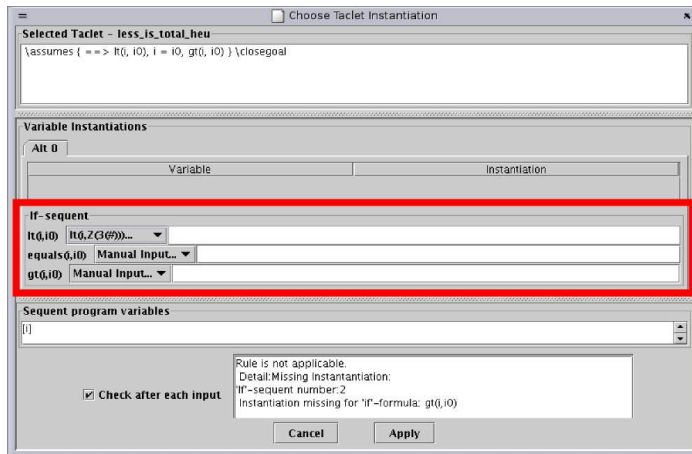




## Schema Variables: Taclet Instantiation Dialog

Primarily two purposes:

- ▶ Provide assumptions of taclet (assumes clause)



## Schema Variables: Taclet Instantiation Dialog

Primarily two purposes:

Drag'n'drop can be used for copying data from sequent view

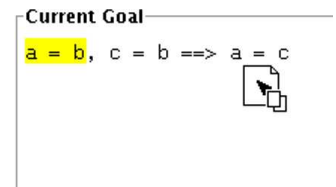
## Applying Taclets using Drag'n'Drop

Possible for taclets with find-part and exactly one assumption, like

- ▶ Rewriting a term using an equation
- ▶ Instantiating formulas with universal-type quantifier

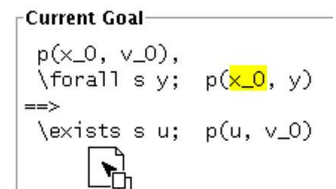
### Applying equations

- ▶ Hold Ctrl, drag the equation to the term to be rewritten



### Instantiating quantified formulas

- ▶ Hold Ctrl, drag instantiation term to quantified formula



## Extension of Proof: Automated Application of Rules

### Selection of active strategy

- ▶ Menu in toolbar

### Invocation of strategies

- ▶ Explicitly ...  
(button in toolbar, context menus in proof tree and sequent view)
- ▶ ... or automatically after each interaction  
(meaningful for strategies *simplifying/normalising* the goals)

### Application of strategies possible on

- ▶ All goals of a proof
- ▶ One particular goal
- ▶ Particular subterm or subformula

## Extension of Proof: Reusing Existing Proof

To Be Done

## “Fundamental” Case Studies: Libraries

### Java Collections Framework (JCF)

- ▶ Part of JCF (treating sets) was specified using UML/OCL
- ▶ Parts of reference implementation were verified
- ▶ It was investigated how the consistency of JCF classes with common algebraic datatypes can be shown

### JavaCard API

- ▶ Most parts of JavaCard API were specified using UML/OCL
- ▶ Some parts of reference implementation were verified

## Security Case Studies: JavaCard Software

### Safety/security properties were treated (specified in dynamic logic)

- ▶ No exceptions are thrown, apart from well-specified ISOExceptions
- ▶ Transactions are properly used (do not commit or abort a transaction that was never started, all started exceptions are also closed)
- ▶ Data consistency (also if a smartcard is “ripped out” during operation)
- ▶ Absence of overflows for integer operations

### Two studies in this area

#### (for which some critical parts were verified)

- ▶ Demoney (about 3000 lines): Electronic purse application provided by Trusted Logic S.A.
- ▶ SafeApplet (about 600 lines): RSA based authentication applet

## Safety Case Studies

### Computation of Railway Speed Restrictions

- ▶ Software by DBSystems for computing schedules for train drivers: Speed restrictions, required break powers
- ▶ Software was formally specified using UML/OCL (based on existing informal specification), verification planned
- ▶ Program translated from Smalltalk to Java
- ▶ Program consists of more than 25 classes

### Command Parser for Chemical Analysis Devices

- ▶ Software by Agilent Technologies
- ▶ Ongoing, Goal: specify parser and verify it
- ▶ Parser originally written in C++: reimplement in MeDeLa, then (automatic) conversion to Java

Part V  
**Wrap-Up**

## Some Current Directions of Research in KeY

- ▶ Multi-threaded Java

Extension of dynamic logic (fixpoints, global induction)  
Granularity of concurrency model  
JCSP implementation ready as prototype

## Some Current Directions of Research in KeY

- ▶ Integration of deduction and static analysis

Mutual call of analyser/prover, common semantic framework  
Implementation of static analysis in theorem proving frame  
Replacing loops with generic proof of body  
Abstraction of verified program on-the-fly

## Some Current Directions of Research in KeY

- ▶ Counter examples

Generate counter example from failed proof attempt  
Counter example search as proof of uncorrectness

## Some Current Directions of Research in KeY

- ▶ Symbolic error propagation

Symbolic error classes modeled by formulas  
Error injection by instrumentation of JavaCardDL rules  
Symbolic error propagation via symbolic execution

## Some Current Directions of Research in KeY

- ▶ Automating of Induction

Simplification of induction claim by code-driven decomposition  
“Rippling” applied to updates guides generalization

## Some Current Directions of Research in KeY

- ▶ Modular verification
- ▶ Verification of MISRA C
- ▶ Proof visualization, proving as debugging

Generation of proof obligations ensuring “global correctness”  
Reduce proof effort by analysing modifiable locations

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